Tutorial Sheets: 0-7

Tutorial sheet No. 0: Revision material on Real numbers

Mark the following statements as True/False:

- (1) $+\infty$ and $-\infty$ are both real numbers.
- (2) The set of all even natural numbers is bounded.
- (3) The set $\{x\}$ is an open interval for every $x \in \mathbb{R}$.
- (4) The set $\{2/m | m \in \mathbb{N}\}$ is bounded above.
- (5) The set $\{2/m | m \in \mathbb{N}\}$ is bounded below.
- (6) Union of intervals is also an interval.
- (7) Nonempty intersection of intervals is also an interval.
- (8) Nonempty intersection of open intervals is also an open interval.
- (9) Nonempty intersection of closed intervals is also a closed interval.
- (10) Nonempty finite intersection of closed intervals is also a closed interval.
- (11) For every $x \in \mathbb{R}$, there exists a rational $r \in \mathbb{Q}$, such that r > x.
- (12) Between any two rational numbers there lies an irrational number.