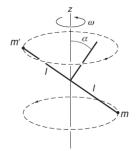
## PH111: Tutorial Sheet 3

This tutorial sheet contains problems related to vector nature of angular velocity, noninertial frames of reference, and pseudo forces.

- 1. A particle is rotating in the xy-plane, along a circular path in counter-clockwise direction, with angular speed  $\omega$ , about the z-axis.
  - (a) Write down the angular velocity of the particle in the vector form, i.e., in terms of components and unit vectors.
  - (b) If the particle is moving along a circle of radius a, write down its position vector  $\mathbf{r}(t)$ , as a function of time, assuming that  $\mathbf{r}(0) = a\hat{\mathbf{i}}$
  - (c) Express its velocity both in Cartesian, and plane polar coordinates
  - (d) Compute the acceleration of the particle both in Cartesian, and plane polar coordinates
- 2. A vector **A** of magnitude *a* is rotating in the *yz* plane in a counter-clockwise manner, with a uniform angular velocity  $\omega$ . It is given that  $\mathbf{A}(t=0) = a\hat{\mathbf{j}}$ .
  - (a) Obtain  $\mathbf{A}(t)$ , as a function of time.
  - (b) Show that  $\frac{d\mathbf{A}}{dt}$  calculated directly, and computed using  $\boldsymbol{\omega} \times \mathbf{A}$ , are the same.
- 3. Consider a simple rigid body consisting of two particles of mass m separated by a massless rod of length 2l. The midpoint of the rod is attached to a vertical axis that rotates at angular speed  $\omega$  around the z axis. The rod is skewed at angle  $\alpha$ , as shown in the figure.



- (a) Calculate the angular momentum  $\mathbf{L}(t)$  of the system, in Cartesian coordinates.
- (b) Verify that  $\frac{d\mathbf{L}}{dt}$  is same as  $\boldsymbol{\omega} \times \mathbf{L}$ .
- 4. A cylinder of mass M and radius R rolls without slipping on a plank which is moving with an acceleration **A**. Calculate the acceleration of the cylinder by analyzing the problem both in the inertial frame and the non-inertial frames. You can use the fact that moment of inertial of a cylinder about its axis is  $\frac{1}{2}MR^2$ .
- 5. A bead of mass m slides without friction on a horizontal rigid wire rotating at constant angular speed  $\omega$  about the z axis.

- (a) Find the distance of the bead from the axis of rotation r(t), as a function of time given that r(0) = 0, and  $\dot{r}(0) = v_0$ .
- (b) What is the force exerted on the bead by the wire.